

Electric rotating machine [Generator]

N.117

* e_{ind} = generated voltage

(1 MV) ...

Gen Induced

Generator action

$$e_{ind} = (\vec{v} \times \vec{B}) \cdot \vec{L}$$

cross product

$$\vec{E} = v \cdot B \cdot \sin \alpha_{vB}$$

$$\alpha_{vB} = 90^\circ \rightarrow E = vB$$

$$E = \left[\frac{n}{s} \frac{V_s}{m^2} = \frac{V}{m} \right]$$

E: electric field

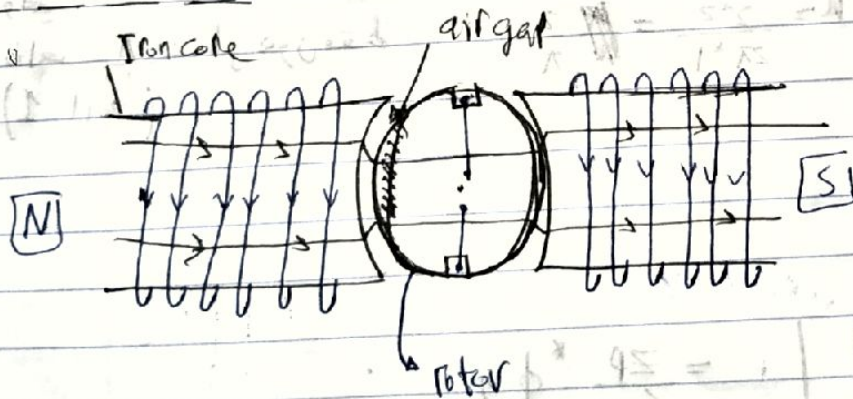
$$B \left[\frac{V_s}{m^2} = \text{Tesla} \right]$$

$$\vec{E} \cdot \vec{L} = E L \cos \alpha = EL = \frac{V}{m} \times n = V$$

$$V \left[\frac{m}{s} \right]$$

$$q_e = -1.6 \times 10^{-19} \text{ As}$$

$$\vec{F} = q * \vec{E} \left[\text{As} \times \frac{V}{m} = \frac{W_s}{m} = N \right]$$



Reluctance

Reluctance Iron

Reluctance air

$$e_{ind} = z v B L$$

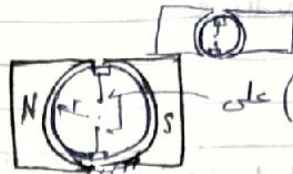
$$e_{ind} (a) = v B L \quad (B) \neq 0 \quad (ca) : v_{BL} \quad (da) = 0 \quad \sum e_{indT} =$$

$$e_{ind} = 2VBL$$

$$A_p = \frac{2\pi rL}{2}$$

area plane for one side
N or S

$$rL = \frac{A_p}{\pi}$$



حسابات (Voltage) على

$$V = \omega r$$

velocity

$$e_{ind} = 2\omega r^* B^* L$$

$$v = 2\omega B r L$$

$$= 2\omega B^* \frac{A_p}{\pi}$$

$$e_{ind} = \frac{2^* \omega}{\pi}^* \phi \quad \left(K = \frac{2}{\pi} \text{ machine constant depend on the geometry of the machine} \right)$$

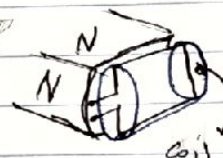
$$e_{ind} = K \phi \omega$$

$$K = \frac{ZP}{2\pi a}$$

C: number of used coils

Nc: turn per coil

$$Z = 2C N_c$$



P: pol-number

a: number of current pole

$$e_{ind} = \frac{ZP}{2\pi a}^* \phi^* \omega$$

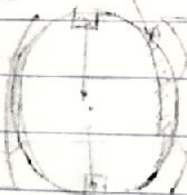
$$Z = 2^* 1^* 1 = 2$$

$$P = 2, a = 1$$

$$K = \frac{2^* 2}{2\pi^* 1} = \frac{2}{\pi}$$

الحسابات (coil 1)

$$e_{ind} = K \phi \omega$$



$$e_{in} = K^* \phi^* \frac{2\pi n}{60}$$

$$= \frac{ZP}{60a}^* \phi n$$

$$= \frac{ZP}{2\pi a} \times \phi \times \frac{2\pi n}{60}$$

$$e_{ind} = K' \phi n \quad \left[K' = \frac{ZP}{60a} \right]$$

Commutator = mechanical rectifier

two contacts (Brushes)

* ال Voltage بطلع A_c ولكن يستخدموا Commutator بقلب عند كل دورة فيقلع
عنا تقريباً ($P < \text{Volt}$)

$$\Phi_e = \frac{P}{2} \Phi_m$$

$$P = 2 \text{ pole} \rightarrow \Phi_e = \frac{2}{2} \Phi_m = \Phi_m$$

* Φ_m هي الدورة الواحدة الكالة فيزيائياً

$$P = 4 \text{ pole} \rightarrow \Phi_e = \frac{4}{2} \Phi_m = 2 \Phi_m$$

* يعني كل دورة بتتغير ال Voltage مرتين

* (Φ_e) هي الدورة الواحدة أو الموجة الواحدة ال Voltage

$$W_e = \frac{P}{2} W_m$$

$$P_e = \frac{P}{2} P_m$$

$$T_e = \frac{2}{P} T_m$$

$$W_e = \frac{P}{2} \times \frac{2\pi n}{60}$$

$$W_e = \frac{P}{2} 2\pi P_m$$

$$\frac{1}{T_e} = \frac{P}{2} \frac{1}{T_m}$$

$$P = 2 \rightarrow T_e = T_m$$

$$2\pi f_e = \frac{P}{2} \times \frac{2\pi n}{60} \rightarrow f_e = \frac{P}{2} \frac{n}{60}$$

$$P = 4 \rightarrow T_e = \frac{2}{4} T_m = \frac{1}{2} T_m$$

$$120 f_e = nP$$

العزل الانسي
الماتور / دائرة التناقلية
Rotor is the armature in the DC machine :

N.120

$$T = K \phi I$$

$$W T = P_{out}$$

$$\frac{2\pi n}{60} \times T = P_{out}$$

$$T = \frac{P_{out}}{(2\pi n/60)}$$

$$Q_{dc} = \frac{P^*}{2} \phi_m$$

if $p = 12 \rightarrow$

$$Q_{dc} = \frac{12}{2} \phi_m = 6 \phi_m$$

$$Q_m = 360^\circ \rightarrow Q_{dc} = \frac{360}{6} = 6^\circ$$

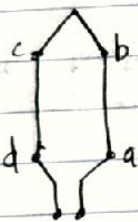
$$e = K \phi \omega$$

$$\rightarrow K' \phi n$$

$$e_{arm} \times I_{out} = P_{out}$$

$$I_{out} = I_{load} = \frac{P_{out}}{e_{dc}} = \frac{P_{out}}{e_{dc}}$$

Armature Windings :



* effective (a-b) و (c-d)
* الماتور يكون خارج المجال المغناطيسي

1 coil turn per coil
 $C=1$ $N_c=3$

$$Z = 2 C N_c$$

$$Z = (2)(1)(3) = 6 \text{ conductors}$$

$$C=1, N_c=1 : Z = 2(1)(1) = 2 \text{ conductors}$$

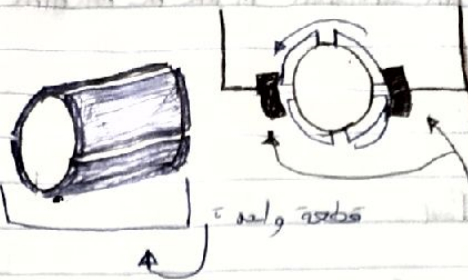
coil turns

[(a-b)(c-d) are conductors]

Winding types of Rotor Coils :

1 - Lap Windings

2 - Wave Windings



مع دوران ال rotor يعكسوا القطبية على سطحه DC

[Lap Winding]



Lap winding : $q = p$

For low voltage and high current machine



أظن ضروري استاذي على R wave
بين يكونا مجاميع اليه على الأرضين

ع (A) في 11.94/1/1
ع (A) في 11.94/1/1

11.94/1/1
11.94/1/1

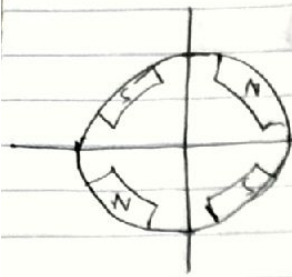
11.94/1/1

11.94/1/1

11.94/1/1

نسبة [1:30] كان في امتحان N. 121

Pol Pitch 180° elect



$$Q_{ele} = \frac{P}{2} Q_m$$

$$W_e t = \frac{P}{2} W_m t$$

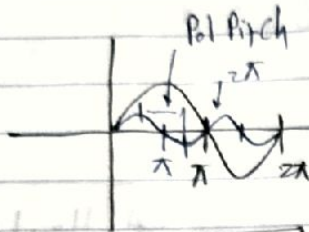
$$3 \pi f_e = \frac{P}{2} 2 \pi f_m$$

$$T_m = 2 T_e$$

$$\frac{1}{T_e} = \frac{P}{2} \frac{1}{T_m}$$

$$P = 4 \rightarrow \frac{1}{T_e} = \frac{2}{T_m}$$

$$T_m = 2 T_e$$



$$P = 4$$

$$\text{Pol Pitch } 180^\circ \text{ elect} = \frac{360^\circ}{P}$$

$$P = 2 = 180^\circ \text{ ele} = \frac{360^\circ}{2} = 180^\circ$$

في كل زاوية 90° من Q_m يكون

هو ال Pol Pitch في كل ربع دائرة

في كل ربع دائرة

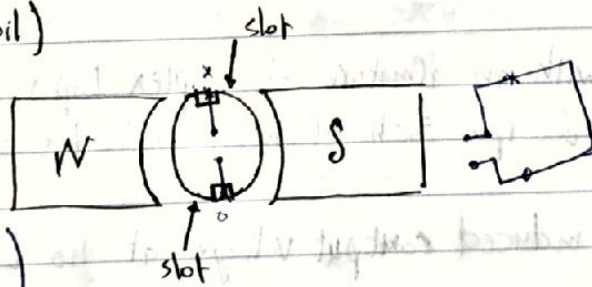
في كل ربع دائرة \cap or \cup or \sim

$$P = 4 \Rightarrow 180^\circ \text{ ele} = \frac{360^\circ}{4} = 90^\circ$$

$$P = 12 \Rightarrow 180^\circ \text{ ele} = \frac{360^\circ}{12} = 30^\circ$$

[Rotor coils]
(Armature coil)

Single Layer winding



1 coil per slot, whatever
was the number of turns

$$C = \frac{1}{2} S_n, S_n = 2 \rightarrow C = 1$$

Doppel Layer Winding

2 coil per each slot whatever was number of turns



coil number

$$C = S_n$$

slot number

$$S_n = 2 \rightarrow C = 2$$

$$S_n = 40 \rightarrow C = 40$$

$$Z = 2 C N_c$$

$$N_c = 8 \text{ turns}$$

$$Z = 2 \times 40 \times 8 = 640 \text{ conductors}$$

Wave Windings

Simplex wave winding; $a = 2$

duplex wave winding; $a = 2m$, $m = 2 \rightarrow a = 4$

$$m = 4 \rightarrow a = 2 \times 4 = 8 \text{ paths or parts}$$

Ex: DC generator with an armature of simplex Lap winding. It has 8 slots 2 poles, driven at $n = 600 \text{ rpm}$ each of Rotor coils has 3 turns the flux $\phi = 0.25 \text{ Vs}$

Determine the induced output voltage at no Load

slot number $S_n = 8$

poles $P = 2$

$n = 600 \text{ rpm}$

turn per coil $N_c = 3 \text{ turns}$

flux $\phi = 0.25 \text{ Vs}$

* Simplex Lap winding ($a = P$)

* single layers winding

$\Rightarrow 2 \text{ poles} = 2 \text{ parts}$

$\Rightarrow 8 \text{ slot} \Rightarrow 4 \text{ coil}$

single = coil per 2 slots

$$Z = 2 C N_c = 2 \times 4 \times 3 = 24 \text{ conductors}$$

جواب!

Simplex Lap winding $a = p$ number of path = number of poles

doublex Lap winding $a = mP$, $m=3$

$$m=2 \rightarrow a = 2^*P, P=2 \rightarrow a=4$$

Triplex Lap winding $m=3 \rightarrow a = 3^*P$

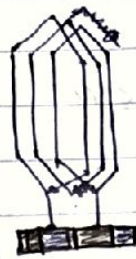
Quadtrex Lap winding $m=4 \rightarrow a = 4^*P$

أعداد الأقطاب

أعداد الأقطاب

نوع، على شكل زخايع

$$\frac{24 \text{ cond}}{8 \text{ slots}} = 3 \text{ cond/slot}$$



3 turns

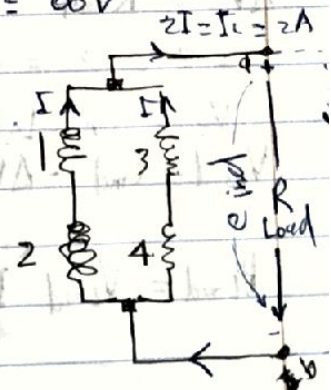


8 slots

Lap winding

$$e_{ind} = \frac{ZP}{2\pi a} \phi \omega = \frac{ZP}{2\pi a} \phi \frac{2\pi n}{60}$$

$$= \frac{ZP}{60} \phi n = \frac{24^*2^*0.25^*600}{60^*2} = 60V$$



2 paths
4 coils

[b] if the generator is loaded by 2A determine the output power given by the generator

$$P_{out} = E_{ind} \cdot I_L = 60 \cdot 2 = 120 \text{ W}$$

* my solution

$$P_{out} = I_A \cdot V_T, \quad V_T = E_A - I_A R_A = 60 - (2)(R_A) \quad P_{out} = I_A \cdot V_T$$

[c] what is the induced torque with respect to [b]

$$T = K \phi I = \frac{ZP}{2\pi q} \phi I = \frac{24 \cdot 2}{2\pi \cdot 2} \cdot 0.25 \cdot 2 = 1.9 \text{ N/m}$$

[d] if each turn has $R_{turn} = 0.01 \Omega$
Determine the power, consumed by the load

$$R_{turn} = 0.01 \Omega$$

$$R_{coil} = 3 \cdot 0.01 = 0.03 \Omega$$

$$R_{branch} = R_{2 \text{ coils in series}} = 2 \cdot 0.03 = 0.06 \Omega$$

branch \rightarrow 2 coils in series, 2 path like x

$$R_{rotor \text{ total}} = \frac{1}{2} \cdot 0.06 = 0.03 \Omega$$

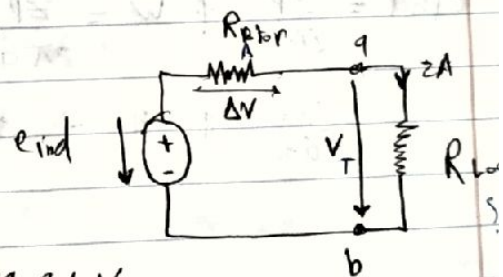
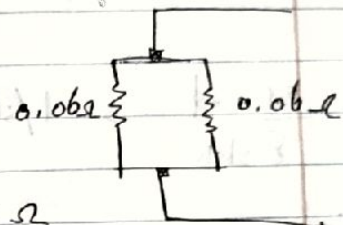
$$\Delta V = 2 \cdot R_{rotor}$$

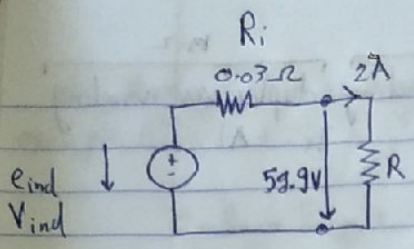
$$= 2 \cdot 0.03 = 0.06 \text{ V}$$

$$V_T = E_A - I_A R_A$$

$$V_{load} = E_{ind} - \Delta V = 60 - 0.06 = 59.94 \text{ V}$$

$$P_{load} = V_{load} \cdot I_{ind} = 59.94 \cdot 2 = 119.88 \text{ W}$$





$$V_T = I_{load} R_{load}, \quad R_{load} = \frac{V_T}{I_A}$$

$$R_L = \frac{59.94}{2} = 29.97 \Omega$$

Example: Wave Winding Rotor of a DC generator (simplex wave), $\phi = 0.25 \text{ V}$
 $N = 600$, $P = 2$ poles, each coil has 3 turns
 8 slots ($N_s = 8$) Single

$$e_{ind} = ? \quad a = 2$$

$$a = 2 \text{ (wave winding simplex)}, \quad C = \frac{1}{2} S_n = \frac{1}{2} * 8 = 4 \text{ coils}$$

$$Z = 2C * N_c = 2 * 4 * 3 = 24 \text{ conductors}$$

$$a = 2 \rightarrow \frac{24}{2} = 12 \text{ cond/path}$$

$$C = 4 \rightarrow \frac{C}{2} = 2 \text{ coil/path}$$

$$1 \text{ coil} = 2C N_c = (2)(1)(3) = 6 \text{ conductors}$$

$$e_{ind} = \frac{ZP}{2\pi a} * \phi * \omega = \frac{ZP}{2\pi a} * \phi * \frac{2\pi n}{60} = \frac{ZP}{60} * \phi * n = \frac{24 * 2 * 0.25 * 60}{60 * 2} = 60 \text{ V}$$

$$R_{turn} = 0.01 \Omega \quad R_{rotor} = \frac{1}{2} * 0.06 = 0.03 \Omega$$

$$R_{coil} = 3 * 0.01 = 0.03 \Omega$$

$$R_{branch} = 2 * 0.03 = 0.06 \Omega$$

